

Heat kernels and non-local Dirichlet forms on ultrametric spaces

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Abstract. We consider a class of jump measures on ultrametric spaces and the associated non-local regular Dirichlet forms. We obtain equivalent conditions for certain heat kernel upper and lower estimates in terms of the properties of the jump measure. In particular, heat kernel estimates are given for quite degenerate/singular jump measures as shown in a number of examples.

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