The P'-operator, the Q'-curvature, and the CR tractor calculus

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Abstract. We establish an algorithm which computes formulae for the CR GJMS operators, the P'-operator, and the Q'-curvature in terms of CR tractors. When applied to torsion-free pseudo-Einstein contact forms, this algorithm both gives an explicit factorisation of the CR GJMS operators and the P'-operator, and shows that the Q'-curvature is constant, with the constant explicitly given in terms of the Webster scalar curvature. We also use our algorithm to derive local formulae for the P'-operator and Q'-curvature of a five-dimensional pseudo-Einstein manifold. Comparison with Marugame's formulation of the Burns-Epstein invariant as the integral of a pseudohermitian invariant yields new insights into the class of local pseudohermitian invariants for which the total integral is independent of the choice of pseudo-Einstein contact form.

Mathematics Subject Classification (2010): 32V05 (primary); 32T15 (secondary).