Existence and concentration of nontrivial solutions for a fractional magnetic Schrödinger-Poisson type equation

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Abstract. We consider the following fractional Schrödinger-Poisson type equation with magnetic fields

$$\varepsilon^{2s}(-\Delta)^s_{A/\varepsilon}u + V(x)u + \varepsilon^{-2t}(|x|^{2t-3} * |u|^2)u = f(|u|^2)u \quad \text{in } \mathbb{R}^3,$$

where $\varepsilon > 0$ is a parameter, $s \in (\frac{3}{4}, 1), t \in (0, 1), (-\Delta)_A^s$ is the fractional magnetic Laplacian, $A : \mathbb{R}^3 \to \mathbb{R}^3$ is a smooth magnetic potential, $V : \mathbb{R}^3 \to \mathbb{R}$ is a positive continuous electric potential and $f : \mathbb{R} \to \mathbb{R}$ is a continuous function with subcritical growth. Using suitable variational methods, we show the existence of a family of nontrivial solutions which concentrates around global minima of the potential V(x) as $\varepsilon \to 0$.

Mathematics Subject Classification (2010): 35A15 (primary); 35R11, 35S05 (secondary).