Automorphisms of surfaces of general type with q = 1 acting trivially in cohomology

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Abstract. Let S be a complex minimal surface of general type with irregularity q(S) = 1 and $\operatorname{Aut}_0(S) \subset \operatorname{Aut}(S)$ the subgroup of automorphisms acting trivially on $H^*(S,\mathbb{Q})$. In this paper we show that $|\operatorname{Aut}_0(S)| \leq 4$, and if the equality holds then S is a surface isogenous to a product of unmixed type. Moreover, examples of surfaces with $|\operatorname{Aut}_0(S)| = 4$ and all possible values of the geometric genus $p_g(S)$ are provided.

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