Ann. Sc. Norm. Super. Pisa Cl. Sci. (5) Vol. XII (2013), 157-187

A T1 criterion for Hermite-Calderón-Zygmund operators on the $BMO_H(\mathbb{R}^n)$ space and applications

Jorge J. Betancor, Raquel Crescimbeni, Juan C. Fariña, Pablo Raúl Stinga and José L. Torrea

Abstract. In this paper we establish a T1 criterion for the boundedness of Hermite-Calderón -Zygmund operators on the $BMO_H(\mathbb{R}^n)$ space naturally associated to the Hermite operator H. We apply this criterion in a systematic way to prove the boundedness on $BMO_H(\mathbb{R}^n)$ of certain harmonic analysis operators related to H (Riesz transforms, maximal operators, Littlewood-Paley g-functions and variation operators).

Mathematics Subject Classification (2010): 42B20 (primary); 42B25, 42B35, 35J10, 42B15, 42C10 (secondary).