# On surfaces of general type with $q=5$ 

Margarida Mendes Lopes, Rita Pardini and Gian Pietro Pirola


#### Abstract

We prove that a complex surface $S$ with irregularity $q(S)=5$ that has no irrational pencil of genus $>1$ has geometric genus $p_{g}(S) \geq 8$. As a consequence, we are able to classify minimal surfaces $S$ of general type with $q(S)=5$ and $p_{g}(S)<8$. This result is a negative answer, for $q=5$, to the question asked in [13] of the existence of surfaces of general type with irregularity $q$ that have no irrational pencil of genus $>1$ and with the lowest possible geometric genus $p_{g}=2 q-3$ (examples are known to exist only for $q=3,4$ ).


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