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On a stronger Lazer-McKenna conjecture for Ambrosetti-Prodi type problems

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Abstract. We consider an elliptic problem of Ambrosetti-Prodi type involving critical Sobolev exponent on a bounded smooth domain. We show that if the domain has some symmetry, the problem has infinitely many (distinct) solutions whose energy approach to infinity even *for a fixed parameter*, thereby obtaining a stronger result than the Lazer-McKenna conjecture.

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