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## Bounds for double zeta-functions

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**Abstract.** In this paper we shall derive the order of magnitude for the double zeta-function of Euler-Zagier type in the region  $0 \leq \Re s_j < 1$  ( $j = 1, 2$ ). First we prepare the Euler-Maclaurin summation formula in a suitable form for our purpose, and then we apply the theory of double exponential sums of van der Corput's type.

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