Galerkin-type methods for strictly parabolic equations on compact Riemannian manifolds

MELANIE GRAF, MICHAEL KUNZINGER AND DARKO MITROVIC

Abstract. We prove existence of weak solutions to the Cauchy problem corresponding to various strictly parabolic equations on a compact Riemannian manifold (M,g). This also includes strictly parabolic equations with stochastic forcing with linear diffusion. Existence is proved through a variant of the Galerkin method and can be used to construct a convergent finite-element method.

Mathematics Subject Classification (2020): 35K65 (primary); 42B37, 76S99 (secondary).