

Nonoccurrence of the Lavrentiev gap for multidimensional autonomous problems

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Abstract. Given a scalar autonomous problem in the multiple integrals calculus of variations, we establish the nonoccurrence of the Lavrentiev gap between Sobolev and Lipschitz maps. The integrand is not assumed to be convex with respect to all variables. The proof relies on a new approximation result for a parametric version of the variational problem.

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