

Partial Gaussian bounds for degenerate differential operators II

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Abstract. Let $A = -\sum \partial_k c_{kl} \partial_l$ be a degenerate sectorial differential operator with complex bounded measurable coefficients. Let $\Omega \subset \mathbb{R}^d$ be open and suppose that A is strongly elliptic on Ω . Further, let $\chi \in C_b^\infty(\mathbb{R}^d)$ be such that an ε -neighbourhood of $\text{supp } \chi$ is contained in Ω . Let $\nu \in (0, 1]$ and suppose that the $c_{kl}|_\Omega \in C^{0,\nu}(\Omega)$. Then we prove (Hölder) Gaussian kernel bounds for the kernel of the operator $u \mapsto \chi S_t(\chi u)$, where S is the semigroup generated by $-A$. Moreover, if $\nu = 1$ and the coefficients are real, then we prove Gaussian bounds for the kernel of the operator $u \mapsto \chi S_t u$ and for the derivatives in the first variable. Finally we show boundedness on $L_p(\mathbb{R}^d)$ of restricted Riesz transforms.

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