

## The entropy of Nakada's $\alpha$ -continued fractions: analytical results

GIULIO TIOZZO

**Abstract.** We study the ergodic theory of a one-parameter family of interval maps  $T_\alpha$  arising from generalized continued fraction algorithms. First of all, we prove the dependence of the metric entropy of  $T_\alpha$  to be Hölder-continuous in the parameter  $\alpha$ . Moreover, we prove a central limit theorem for possibly unbounded observables whose bounded variation grows moderately. This class of functions is large enough to cover the case of Birkhoff averages converging to the entropy.

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