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## The Extended Future Tube Conjecture for $\mathrm{SO}(1, n)$

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**Abstract.** Let  $C$  be the open upper light cone in  $\mathbb{R}^{1+n}$  with respect to the Lorentz product. The connected linear Lorentz group  $\mathrm{SO}_{\mathbb{R}}(1, n)^0$  acts on  $C$  and therefore diagonally on the  $N$ -fold product  $T^N$  where  $T = \mathbb{R}^{1+n} + iC \subset \mathbb{C}^{1+n}$ . We prove that the extended future tube  $\mathrm{SO}_{\mathbb{C}}(1, n) \cdot T^N$  is a domain of holomorphy.

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